

Measuring the Temperature of Hot Nuclear Fragments

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Abstract

A new thermometer based on fragment momentum fluctuations is presented. This thermometer exhibited residual contamination from the collective motion of the fragments along the beam axis. For this reason, the transverse direction has been explored. Additionally, a mass dependence was observed for this thermometer. This mass dependence may be the result of the Fermi momentum of nucleons or the different properties of the fragments (binding energy, spin etc..) which might be more sensitive to different densities and temperatures of the exploding fragments. We expect some of these aspects to be smaller for protons (and/or neutrons); consequently, the proton transverse momentum fluctuations were used to investigate the temperature dependence of the source.

Keywords: nuclear reactions, temperature, phase transition, caloric curve, projectile fragmentation

1. Introduction

For many years, various thermometers have been used to expand the experimental understanding of nuclear systems. These studies have often been motivated by the desire to define the proposed nuclear liquid-gas phase transition [1, 2, 3]. A broad array of caloric curves have been obtained allowing a better understanding of the nuclear limiting temperature and its dependence on source excitation energy as well as source size [4]. Additionally, nuclear thermometry has provided a bridging connection between isoscaling [5, 6, 7] and the symmetry coefficient of the nuclear equation of state [8].

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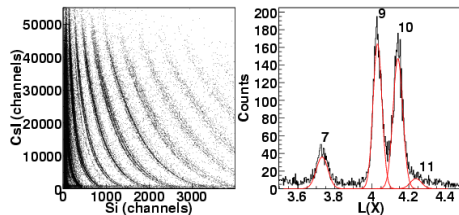


Figure 1: Left: Raw data from ΔE -E with Si-CsI detectors. Right: Projected, linearized data for $Z=4$ isotopes. The x-axis is L_X , which is the linearized value. (color online)

Several thermometers have been used extensively in nuclear studies. In many studies, the nuclear temperature has been obtained from energy spectra through moving source fitting [10, 11, 12]. However, this thermometer is known to exhibit non-thermal and collective behavior [13]. Alternatively, temperature may be obtained through isotopic thermometers [14]. The double isotope thermometer has provided much data [18, 15, 16, 17], however the temperatures derived are complicated by model dependent secondary decay corrections [17, 19]. Ratios of excited states may also be used to obtain temperature for low to mid excitation energies [2].

2. Experimental

In this work, we seek to measure the temperature of reconstructed quasi-projectiles from the reactions of $^{86,78}\text{Kr} + ^{64,58}\text{Ni}$ at 35 MeV/nucleon collected with the NIMROD-ISiS array [20, 21] at Texas A&M University. The NIMROD-ISiS array is a 4π charged particle array housed inside the TAMU Neutron Ball. This experimental hardware configuration provides free neutron data in conjunction with isotopically resolved charged particle event reconstruction. The data presented in this paper was extracted from particles detected in the silicon detectors in rings 2-9 and the CsI detectors in rings 2-11.

There are three possible sources of fragment charge and mass identification in NIMROD-ISiS. Pulse shape discrimination of the CsI fast versus slow light output was used for $Z=1,2$. The ΔE -E method is used for $Z \geq 3$ on Si-Si and Si-CsI. The particle identification was done through linearization of the raw data [21] to remove the non-trivial curvature due to energy deposition characteristics of the detection methods (see left panel of Fig. 1). The linearization utilized lines carefully chosen to follow the strongest isotope of each element. The data were then straightened using a calculation of the distance between the data point and two closest chosen lines.

After linearization, data were projected onto an axis, $L(x)$, producing quasi-Gaussian peaks. The isotopic peaks in the projected distributions were fitted with Gaussian functions. The fragment charge was assigned by limits placed on the linearization x-axis value (L_X). The mass of each particle was assigned by determining the probability of the particle belonging to a given isotope.

This probability (P_A) was calculated by comparing the value of the isotopic Gaussian functions at the L_X value of the particle

$$P_A = \frac{G_A(L_X)}{\sum_i G_i(L_X)} \quad (1)$$

where G_A is the fitted Gaussian to the selected isotope which is compared to the summation over all Gaussian functions (G_i) defined for the element. For this data, a mass was defined only if the P_A was ≥ 0.75 . This method of fitting the linearized data with Gaussian functions provided the ability to estimate the average contamination between neighboring isotopes. The average contamination in the yield of a given isotope as defined here was calculated to be $\approx 5\%$ across all reaction systems and all detectors. Example linearized projections of Be fragments are plotted in the right panel of Fig. 1.

The quasi-projectile source was selected by means of several event-by-event cuts on the experimental data. The first cut required that the sum of the collected charged fragments ($\sum Z$) for the event equal a minimum of $Z=30$. The fragments in an accepted event were then cut on the longitudinal velocity relative to the largest fragment [22]. This cut varied with the fragment Z . The fragments retained for $Z=1$, $Z=2$, and $Z \geq 3$ had to have longitudinal velocities within the range of $\pm 65\%$, 60% , 40% , respectively, of the largest fragment longitudinal velocity. The sum of the charges of the collected and accepted fragments was again constrained to be in the range $Z=30-34$. Limits were placed on the deformation of the source by means of a cut on the quadrupole moment of the momentum distribution [23].

This method of source definition was compared to events and fragments generated by the HIPSE-SIMON code [24]. The initial $\sum Z$ cut eliminates a significant number of incomplete events and events from other sources. This cut, however, was not sufficient to eliminate all fragments resulting from mid-velocity or pre-equilibrium sources. The fragment velocity cut successfully helped minimize fragments from non-projectile-like sources. The final cut on the deformation provided a reasonable level of isotropy in the selected events.

After the quasi-projectile source was defined, the event excitation energy was calculated using:

$$E_{source}^* = \sum_i^{M_{cp}} K_{cp}(i) + M_n \langle K_n \rangle - Q_{gg}. \quad (2)$$

The excitation energy (E_{source}^*) was defined as the sum over the accepted particles center of mass kinetic energy (K_{cp} and K_n) minus the reaction Q-value. The average kinetic energy of the neutrons was calculated as the proton average kinetic energy with a correction for the Coulomb barrier energy [25].

Proper calculation of the excitation energy should include the neutron and gamma energy corrections. The Neutron Ball provides an experimental neutron multiplicity per event that must be corrected for background, neutron source,

and efficiency. The multiplicity of free neutrons was extracted from the experimental quasiprojectile (Q_p) data using:

$$M_{QP} = \frac{M_{exp} - M_{bkg}}{(\epsilon_{QP} + \frac{N_T}{N_P} \epsilon_{QT})(.7/.6)}. \quad (3)$$

The multiplicity of neutrons assigned to the projectile source (M_{QP}) was calculated from the background (M_{bkg}) corrected experimental neutron multiplicity (M_{exp}). and corrected using the relative efficiency of the Neutron Ball for detecting free neutrons emitted from a quasi-projectile (ϵ_{QP}) and quasi-target (ϵ_{QT}) sources for this reaction. The free neutron correction also accounted for the total neutron contributions from both the target (N_T) and projectile (N_P) nuclei. The efficiencies were extracted from tagged neutrons generated by the HIPSE-SIMON code and the GEANT3 [26] simulation of the detector [20]. Simulation and filtering provided $\epsilon_{QP}=0.65$ and $\epsilon_{QT}=0.40$. The Neutron Ball was calibrated with a ^{252}Cf source to 70% efficiency for this experiment. The correction factor in the denominator accounts for the experimental calibration of the Neutron Ball to 70% efficiency rather than the 60% efficiency obtained from the GEANT3 simulation of the detector. Event by event, the M_{QP} provided an estimate of the free neutrons emitted from the quasi-projectile.

The energy carried away by gammas is generally considered to be small [18, 27]. In an effort to account for gamma energy, the ISiS collaboration calculated $E_\gamma = 1\text{MeV}(M_{Z \geq 3})$ [27]. However, this energy has not been constrained experimentally [28]. Using this formula the gamma energy is $\leq 1\%$ of the total excitation energy of these events. The gamma energy correction is not included in calorimetry of this data as it is small compared to that of the excitation energy and is poorly constrained.

3. Temperature determination with the momentum fluctuation thermometer

A new method of calculating the system temperature can be derived from the momentum fluctuations of particles in the center of mass frame of the fragmenting source. In this case, the frame is that of the reconstructed quasi-projectile. The momentum is constructed for each particle in the projectile frame center of mass for each axis. The momenta are then compared using Eq. 4:

$$\begin{aligned} Q_x &= 2P_x^2 - P_y^2 - P_z^2 \\ Q_y &= 2P_y^2 - P_x^2 - P_z^2 \\ Q_z &= 2P_z^2 - P_x^2 - P_y^2 = 2P_z^2 - P_T^2 \\ Q_{xy} &= P_x^2 - P_y^2 \end{aligned} \quad (4)$$

where P_x , P_y , and P_z are the momenta in the X,Y and Z-axis respectively of each particle. The Q distributions extracted from equation 4 for the longitudinal (Q_z) and transverse (Q_{xy}) are shown in figure 2. In an ideal, spherical,

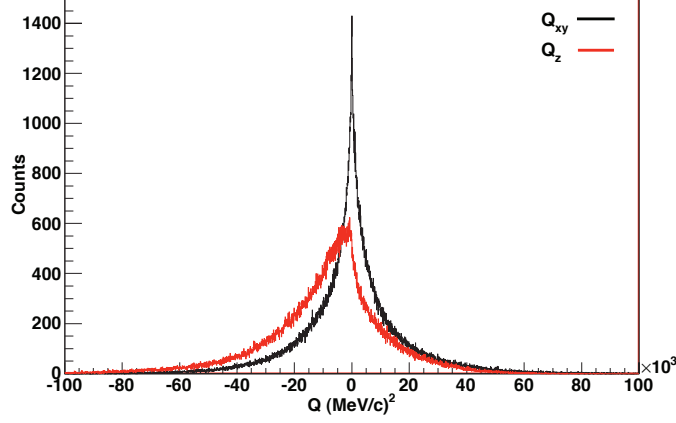


Figure 2: Q_z and $Q_{x,y}$, Q distributions extracted from equation 4 for the longitudinal (Q_z) and transverse (Q_{xy}) calculated using all fragments. (color online).

fragmenting source the sum of Q for all fragments in the event in the center of mass of that event should be a δ function at zero. However, in a real system fluctuations occur within a class of events. These fluctuations convert the momentum δ function into a distribution that can be characterized by a mean and width. In an equilibrated system, the mean should still equal zero.

The variance (σ^2) may be obtained from the Q_z distribution through

$$\sigma^2 = \langle Q_z^2 \rangle - \langle Q_z \rangle^2 \quad (5)$$

where Q_z is the quadrupole moment (Eq. 4). If the mean equals zero, the second term cancels. Taking the first term as

$$\langle Q_z^2 \rangle = \int d^3p (2P_Z^2 - P_T^2)^2 f(p) \quad (6)$$

and assuming a Maxwellian distribution of the momentum yields

$$\langle Q_z^2 \rangle = \frac{1}{(2\pi mT)^{3/2}} \int d^3p (4P_Z^4 - 4P_Z^2 P_T^2 + P_T^4) e^{-\frac{P_Z^2 + P_X^2 + P_Y^2}{2mT}}. \quad (7)$$

A Gaussian integral is used

$$I_n(a) = \int_0^\infty x^n e^{-ax^2} dx \quad (8)$$

and the results that are of interest to this derivation are:

$$I_0(a) = \frac{1}{2} \sqrt{\frac{\pi}{a}} \quad (9)$$

$$I_2(a) = \frac{1}{4a} \sqrt{\frac{\pi}{a}} \quad (10)$$

$$I_4(a) = \frac{3}{8a^2} \sqrt{\frac{\pi}{a}}. \quad (11)$$

It is important to note that these integrals are only for 0 to ∞ and therefore should be doubled for $-\infty$ to ∞ . After derivation, the relation between variance and temperature becomes:

$$\sigma^2 = 4 \left(\frac{3}{4a^2} \right) - 4 \left(\frac{1}{2a^2} \right) + \frac{2}{a^2} = 12m^2T^2. \quad (12)$$

where

$$a = \frac{1}{2mT} \quad (13)$$

For a single fragment type from a nuclear multi-fragmentation:

$$\sigma^2 = 12A^2m_0^2T^2 \quad (14)$$

where m_0 is the mass of a nucleon and A is the mass number of the fragment. For multiple particle types, the formula becomes:

$$\sigma^2 = 12m_0^2T^2 \sum_i (\zeta_i A_i)^2 \quad (15)$$

where ζ is the concentration of the particle in question. A similar derivation can be carried out using Q_x and Q_y defined in Eq. 4.

Because of the velocity source cuts, the Z-axis does not exhibit the same momentum distributions as are seen in the X,Y-axes. Therefore, the temperature was re-derived using only the P_x and P_y momentum and employing the same Maxwellian distribution and Gaussian integral assumptions. Here Q_{xy}^2 is defined as

$$Q_{xy}^2 = \int d^2p (P_X^4 - 2P_X^2 P_Y^2 + P_Y^4) f(p) \quad (16)$$

and using the Maxwellian distribution assumption gives:

$$\sigma^2 = 4m^2T^2. \quad (17)$$

For a single fragment type from a nuclear multi-fragmentation:

$$\sigma^2 = 4A^2m_0^2T^2 \quad (18)$$

where m_0 is the mass of a nucleon and A is the mass number of the fragment. For multiple fragment types,

$$\sigma^2 = 4m_0^2T^2 \sum_i (\zeta_i A_i)^2 \quad (19)$$

where ζ is again the concentration of a given particle type. The temperature is now linked to the variance through Eqs. 15 and 19. The temperature evaluated

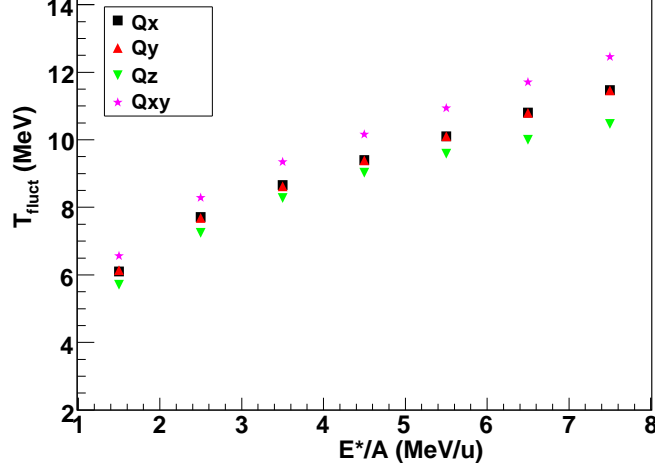


Figure 3: Q_x , Q_y , Q_z and Q_{xy} (Eqs. 4 and 18) temperatures (Eqs. 15 and 19) calculated using all fragments as a function of E^*/A of the source event. (color online).

from all fragments assigned to the quasi-projectile fragmentation event is shown in Fig. 3 for the quadrupole oriented along various axes (Q_z, Q_x, Q_y) as well as the transverse quadrupole (Q_{xy}) (Eq. 4). These quantities should be exactly the same in a thermally equilibrated system, any deviation from thermal equilibrium will be disclosed from the differences in the quantity Q calculated along different axes. The statistical error bars are smaller than the size of the points in Fig. 3. The Q_x , Q_y thermometers are identical within errors and the Q_z thermometer is slightly lower due to the longitudinal velocity cuts imposed as part of the quasiprojectile source selection. The transverse thermometer based on Q_{xy} provides a higher source temperature across all excitation energies than was obtained using the Q_x , Q_y , or Q_z thermometers. This difference in temperature is the result of eliminating the effect due to the velocity cuts along the Z-axis. Hence it is imperative to investigate the temperature extracted from the transverse velocity of the fragments.

The momentum distributions may also be widened by recoil during the source break up. The recoil effect on the momentum Q distributions has been parameterized as

$$Q_{xy(0)} = Q_{xy(app)} \left(\frac{A - A_f}{A - 1} \right) \quad (20)$$

where $Q_{xy(0)}$ is the recoil corrected value, $Q_{xy(app)}$ is the experimental value (Eq. 19), A is the mass of the source, and A_f is the mass of the fragment being considered [13].

Combining all of the fragments together to create a Q distribution depends on the assumption that all of the fragments, regardless of mass or charge, have

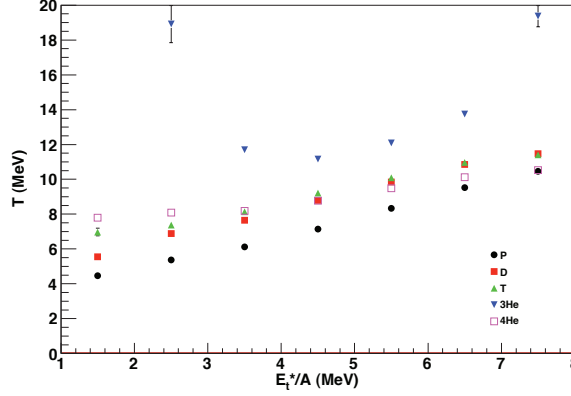


Figure 4: Apparent temperatures extracted from the Q_{xy} distributions as a function of particle type. (color online)

the same distribution width. This implies a simultaneous, statistical emission of fragments. The apparent temperatures obtained from the recoil corrected Q_{xy} distributions as a function of particle type and source excitation energy are plotted in Fig. 4. Though the temperature increases with excitation energy regardless of particle type, there is a significant spread in measured temperature across the fragment types.

A significant mass dependence at constant Z may be seen in the $^3,^4\text{He}$ isotopes. The ^3He yields a $\sim 35\%$ higher temperature than the ^4He across all E^*/A . The ^4He apparent temperatures show a $\sim 15\%$ increase across $E^*/A = 1.5-7.5$. The ^3He temperatures, on the other hand, increase by $\sim 50\%$ across the same E^*/A region. It is possible that some of the mass dependence of the apparent temperature is the result of differential fragment emission time. It is known that ^3He is emitted early in the fragmentation process. Conversely, ^4He is emitted throughout the de-excitation cascade [29]. The difference in measured temperature seen in the $A=3$ isotopes may indicate a Coulomb contribution to the momentum distributions widths. On the other hand the results for ^2H and ^4He isotopes rules out a strong Coulomb dependence of T . Other authors results [3] suggest that Coulomb is not so important in our beam energy region.

In addition to the above mentioned factors, the temperature obtained with this thermometer could be a combination of thermal energy and Fermi momentum in the detected fragments [13]. Following the paper of Bauer, the measured fragments exhibit a momentum distribution resulting not only from thermal sources, but also from the Fermi momentum of the component nucleons with the fragment. This effect increases as a function of fragment size until a limiting value is observed. This correction is only meaningful for fragments with $A \geq 2$. Thus, the momentum distributions of protons are free of this complication.

The caloric curve derived from the proton momentum fluctuation widths of

the $^{86}\text{Kr}+^{64}\text{Ni}$ system is plotted in Fig. 5 (top panel). The fluctuations for this thermometer include the Z-axis, eq.(16), thus include collective effects if any. For reference, the compilation of Natowitz *et al.* [4] and two Fermi Gas curves ($T = \sqrt{E^*/a}$ with $a = A/8, A/13 \text{ MeV}^{-1}$) are plotted. As shown in this figure, the protons produce temperatures similar to what is obtained from a Fermi Gas at low E^*/A indicating that this thermometer does indeed yield reasonable temperature values. The errors plotted in Fig. 5 for the Y-axis are estimated systematic errors of 0.5 MeV.

As discussed above the quadrupole fluctuations displayed a nonequilibrium effect still present along the beam direction. We expect these effects to be present in the determination of the excitation energy as well. To a first approximation we can correct for this nonequilibrium effect by replacing the kinetic energy of the fragments in eq.(2) by its transverse component. i.e. : $K_{cp} \rightarrow 3/2 K_{T_{cp}}$, similarly for neutrons. The excitation energy determined from the transverse kinetic energy of the fragments is approximately 0.3 to 0.5 MeV larger than that which is determined by the total kinetic energy, see Fig. 5 (bottom panel). As we see in the figure, the difference when the transverse energy and the 'transverse' temperature are used becomes quite important for increasing excitation energies where collective effects become more important. Interestingly the 'caloric curve' obtained without collective effects shows a back bending similar to what was predicted by D. Gross long ago[31]. This might be a signature for a phase transition as discussed in [32, 31], however a more detailed study of this feature is beyond the goal of this paper and will be discussed in more detail in a future publication.

When the collective motion is removed the transverse temperature rises from approximately 4 MeV to 10 MeV over this excitation energy range. Slope "temperatures" were also extracted from this data set by fitting the kinetic energy spectra[33] of the fragments. Both the quadrupole temperature and the slope temperature are derived from the kinetic energy. However the quadrupole temperature should be less susceptible to secondary decay and non-equilibrium effects. Since the velocity cuts imposed to minimize the effect of the non-equilibrated motion in the beam direction mainly affect the $Z=1$ and $Z=2$ particles, the slope temperatures extracted from the fits to the kinetic energy spectra for $Z \geq 3$ should not be impacted. The values of the slope temperature were consistently approximately 3 MeV higher than those extracted from the quadrupole temperature. As already mentioned the fragment kinetic energy spectra are a result of both thermal energy and Fermi momentum[13]. Thus this comparison may contain important information about the contribution from the Fermi momentum and will be the subject of future works.

We expect that at low T or excitation energy the Fermi gas formula $E^* = aT^2$ should be valid, see Fig.5. Thus it is convenient to plot the quantity E^*/aT^2 versus T to see any deviation from a pure Fermi gas. In Fig (6) we plot the reduced excitation energy versus temperature as derived from the transverse kinetic energy of the fragments (full squares) as well as the total kinetic energy of the fragments (open squares). As seen in the figure at small T the two results are identical within the error bars. For increasing T the two results differ

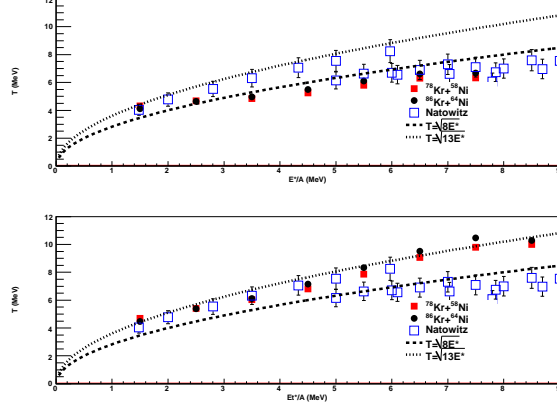


Figure 5: Q_z (Eq. 4) temperatures derived from proton momentum fluctuations as a function of E^*/A of the source event. For reference the caloric curve for $A=60-100$ from the Natowitz compilation [4] as well as two Fermi Gas ($T = \sqrt{aE^*/A}$ with $a = 8, 13$) curves are plotted (Top panel). (Bottom panel) same as above but for the corresponding 'transverse' quantities. (color online)

much demonstrating the increased influence of the non-equilibrium effects with increasing T or excitation energy. The back bending is now more pronounced compared to fig. 5.

The values obtained from the transverse energy have been normalized to 1 at the lowest measured temperature using a level density parameter $a_0 = A/13.3 \text{ MeV}^{-1}$. We notice that such a quantity is density dependent i.e. $a = a_0(\rho_0/\rho)^{2/3}$. From this relation, assuming that the nuclear Fermi gas is reaching different densities at different temperatures [34, 35, 36], we can deduce a value of density for each measured temperature. We can easily calculate the density at each temperature by noticing that:

$$\frac{\rho}{\rho_0} = \left(\frac{a_0 T^2}{E^*} \right)^{3/2} \quad (21)$$

The validity of the Fermi gas model is related to the ratio of the temperature to the Fermi energy $T/\epsilon(\rho)_F$. If the density decreases also the Fermi energy decreases as: $\epsilon(\rho)_F = 36(\rho/\rho_0)^{2/3} \text{ (MeV)}$. Where 36 MeV is the Fermi energy of the nucleus ground state and we are assuming to be the same value at the smallest measured temperature. Since we can estimate the change of density for each temperature we can also obtain a value for the Fermi energy. In figure (7) we plot the reduced density versus the reduced T (i.e. divided by the corresponding Fermi energy). As we see in the figure the values of the reduced temperature are well below 1 which implies that our Fermi gas approximation is valid and the system is a quantum Fermi system even at the highest measured temperatures. This is at variance with many authors which assume that the

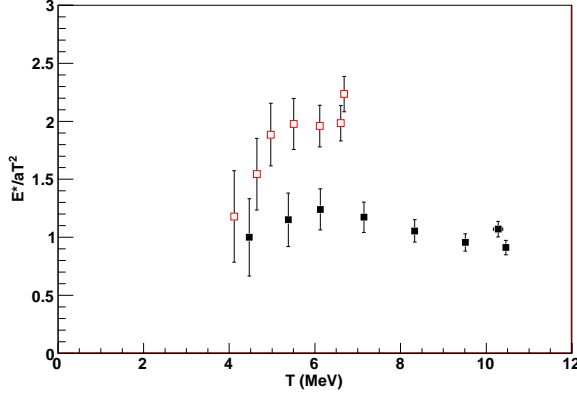


Figure 6: E^*/aT^2 vs T derived from the transverse kinetic energy of the fragments (full squares) and the total kinetic energy (open squares) for the $^{86}\text{Kr} + ^{64}\text{Ni}$ system. (color online)

system is classical at the highest measured temperature[30]. More important, the result without collective effects suggests that the density is roughly constant in the range of temperatures considered at variance with the analysis which includes collective effects. The latter case would suggest an expanding system at all temperatures while the previous case enforces the concept of freeze out volume. If this conjecture will be confirmed by future analysis we could study the nuclear equation of state at (almost) constant density.

If the picture of an expanding system with increasing temperature is correct, a caloric curve as the one of figures (5) and (6) might be misleading. A different physical interpretation of the caloric curve could result if we plot opportunely normalized quantities as in figure(8). In these units the 'apparent' saturation of the temperature at high excitation energies now disappears because of the changing density of the system contained in the Fermi energy and the level density parameter. In contrast the results with non-equilibrium effects removed display a more remarked back bending. We stress that these results are derived assuming a Fermi gas relation and are for sake of discussion. A more precise determination of the equation of state requires a more complete determination of the quantities at play, i.e. excitation energy, temperature and density (or pressure) of the system.

4. Concluding remarks

Four momentum thermometers have been defined here (Eqs. 4, 19). The first three (Q_x , Q_y , and Q_z) should theoretically be degenerate. However, the Z-axis was found to be truncated by the source selection. This affected all three of these thermometers. To remove this characteristic along the Z-axis, the

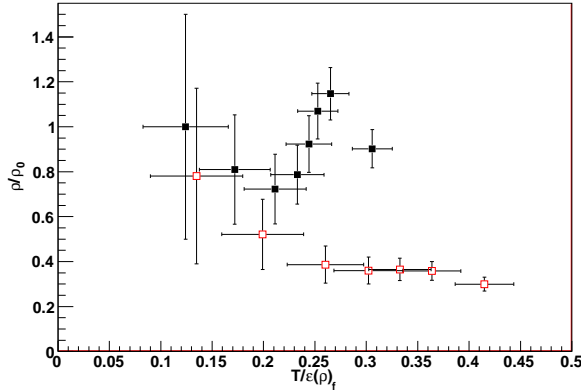


Figure 7: Reduced density vs reduced temperature derived for a Fermi gas from the transverse kinetic energy of the fragments (full squares) and the total kinetic energy (open squares) for the $^{86}\text{Kr} + ^{64}\text{Ni}$ system. (color online)

temperature was then derived using only the X and Y-axes. This thermometer provides a slightly higher temperature reflecting the removal of the Z-axis with its incorrect width. The high value of T obtained from this thermometer may be a result of Fermi momentum in the fragments. This effect is zero for protons. The proton caloric curve is shown in Fig. 5. Since a non-equilibrium effect is present in the temperature determination, we have also suggested a method to reduce the non-equilibrium effects in the determination of the excitation energies by using the transverse kinetic energy of the fragments. The modified caloric curve thus obtained has been discussed in Fig. 5 demonstrating the increased importance of collective effects at high system temperatures (or excitation energies). Assuming a Fermi gas relation for an expanding system we have been able to derive a density value for each temperature. From the density we can estimate the corresponding Fermi energy and demonstrated that the system is still a quantum Fermi system at the current temperatures and densities. We stress that the assumption of an expanding Fermi gas is suggested by some microscopic calculation [30], but it is at variance with some statistical models which assume a constant freeze-out density [32]. If a constant density is the correct picture then the best representation of the caloric curve would be the ones of Fig. 5 and Fig. 6 while if density is changing we should refer to Fig. 8. In both cases we do not expect the densities to be dramatically different from those estimated in Fig.7 which implies that we are in a quantum regime at all temperatures.

Which picture of fragmentation is correct will probably be debated both experimentally and theoretically in future years. To this debate we have to add the observation that our proposed method gives different temperatures for different fragments. The origin of this difference could be in the statistics of

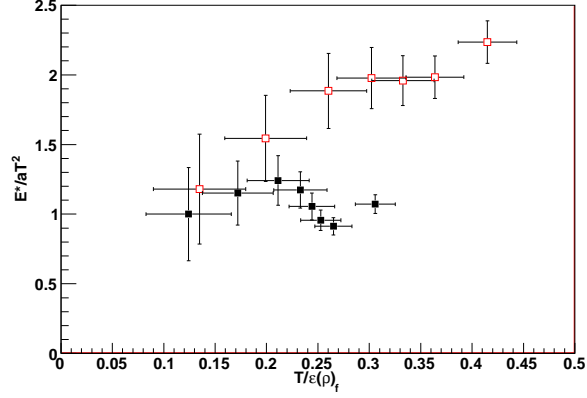


Figure 8: Caloric curve in reduced units for the $^{86}\text{Kr} + ^{64}\text{Ni}$ system. Full squares are from the transverse kinetic energy of the fragments and the open squares are using the total kinetic energy. (color online)

the fragments (i.e. Bose versus Fermi systems), in different Coulomb charges or time of creation including evaporation. Other proposed thermometers also suffer from this isotope dependence of the temperature. These features should be resolved in order to gain full understanding of an excited quantum nuclear system.

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